

UPPER AND LOWER WEAKLY (τ, m) - J -CONTINUOUS MULTIFUNCTIONS

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ABSTRACT. We introduce the notions of upper/lower weakly (τ, m) - J -continuous multifunctions and obtain some characterizations of such multifunctions. These concepts are obtained using different generalizations of the notion of J -open sets on the ideal topological space (Y, σ, J) .

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